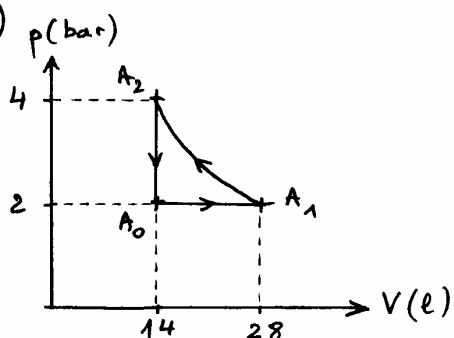


1) a)



b)  $p_1 V_1 = n R T_1$

$$\Rightarrow T_1 = \frac{p_1 V_1}{n R} = \frac{2 p_0 V_0^m}{R} = 673,562654$$

$$T_1 = 674 \text{ K}$$

$p_2 V_2 = n R T_2$

$$\Rightarrow p_2 = \frac{n R T_2}{V_2} = \frac{R T_1}{V_0^m} = 400000$$

$$p_2 = 4,00 \cdot 10^5 \text{ Pa} = 4,00 \text{ bar}$$

2)  $A_0 \rightarrow A_1$  transfo isobare

$$Q(A_0 \rightarrow A_1) = \Delta H(A_0 \rightarrow A_1) = C_p (T_1 - T_0) = \frac{n R \gamma}{\gamma - 1} (T_1 - T_0) \quad \text{or } n = 1 \text{ mol}$$

$$Q(A_0 \rightarrow A_1) = \frac{R \gamma}{\gamma - 1} (T_1 - T_0) = 9,80 \text{ kJ}$$

A.N.  $T_0 = 336,7813327 = 337 \text{ K}$

$Q = 9800,000 \text{ J}$

$$W(A_0 \rightarrow A_1) = - \int_0^1 p dV = - p_0 (V_1 - V_0) = - p_1 V_1 - p_0 V_0 = - n R (T_1 - T_0)$$

$$W(A_0 \rightarrow A_1) = - R (T_1 - T_0) = -2800,000 \text{ J} = -2,80 \text{ kJ}$$

 $A_1 \rightarrow A_2$  transfo isotherme

$\Delta U(A_1 \rightarrow A_2) = 0 = W + Q$

$$W(A_1 \rightarrow A_2) = - \int_1^2 p dV = - n R T_1 \ln \frac{V_2}{V_1} = - R T_1 \ln \frac{V_0^m}{2 V_0^m}$$

$$W(A_1 \rightarrow A_2) = R T_1 \ln 2 = 3,88 \text{ kJ} \quad (3881,624 \text{ J})$$

$$Q(A_1 \rightarrow A_2) = - R T_1 \ln 2 = -3,88 \text{ kJ}$$

 $A_2 \rightarrow A_0$  transfo isochore

$$Q(A_2 \rightarrow A_0) = \Delta U(A_2 \rightarrow A_0) = C_v (T_0 - T_2)$$

$$Q(A_2 \rightarrow A_0) = \frac{R}{\gamma - 1} (T_0 - T_1) = -7000,000 \text{ J} = -7,00 \text{ kJ}$$

$$W(A_2 \rightarrow A_0) = 0$$

3) Le premier principe sur le cycle s'écrit  $\Delta U = 0$ 

$$\Delta U = W(A_0 \rightarrow A_1) + W(A_1 \rightarrow A_2) + W(A_2 \rightarrow A_0) + Q(A_0 \rightarrow A_1) + Q(A_1 \rightarrow A_2) + Q(A_2 \rightarrow A_0)$$

$$= -R(T_1 - T_0) + R T_1 \ln 2 + 0 + \frac{R \gamma}{\gamma - 1} (T_1 - T_0) - R T_1 \ln 2 + \frac{R}{\gamma - 1} (T_0 - T_1)$$

$$= \left( \frac{R \gamma}{\gamma - 1} - R - \frac{R}{\gamma - 1} \right) (T_1 - T_0) = \frac{R}{\gamma - 1} (\gamma - \gamma + 1 - 1) (T_1 - T_0)$$

$$\Delta U = 0$$

le premier principe est vérifié